

**The University Interscholastic League  
Number Sense Test, Series 990A**

	Score	Initials
Final		
1st		
2nd		

Contestant's Number \_\_\_\_\_

**Read Directions Carefully  
Before Beginning Test**

**Do Not Unfold This Sheet  
Until Told To Begin**

**DIRECTIONS:** Do not turn this page until the person conducting this test gives the signal to begin. This is a ten-minute test. There are 80 problems. Solve accurately and quickly as many as you can in the order in which they appear. **ALL PROBLEMS ARE TO BE SOLVED MENTALLY.** Make no calculations with paper and pencil. Write only the answer in the space provided at the end of each problem. Problems marked with a (\*) require approximate integral answers; any answer to a starred problem that is within five per cent of the exact answer will be scored correct; all other problems require exact answers.

The person conducting this contest should explain these directions to the contestants.

**Stop - Wait for Signal!**

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| <p>(1) <math>1999 \times 200 =</math> _____</p> <p>(2) <math>514 \div 5 =</math> _____ (decimal).</p> <p>(3) <math>25 \times 143 =</math> _____</p> <p>(4) <math>562 - 265 =</math> _____</p> <p>(5) Which smaller, <math>\frac{5}{7}</math> or <math>\frac{7}{9}</math>? _____</p> <p>(6) <math>1257 \div 9 =</math> _____ (mixed number).</p> <p>(7) <math>745 + 547 =</math> _____</p> <p>(8) <math>22 \times 22 =</math> _____</p> <p>(9) <math>11 + 12 \times 13 - 14 =</math> _____</p> <p>*(10) <math>103 + 108 + 115 + 124 + 135 =</math> _____</p> <p>(11) 12% of <math>35 + 15 =</math> _____</p> <p>(12) <math>15 \times 18 + 30 \times 9 =</math> _____</p> <p>(13) <math>16 - 12 - 8 - 4 - 1 =</math> _____</p> <p>(14) <math>5(4) + 43(5) + 6(9) =</math> _____</p> <p>(15) The LCM of 48 and 36 is _____</p> <p>(16) <math>17 \times 37 =</math> _____</p> <p>(17) 1.5% = _____ (fraction).</p> <p>(18) <math>23 \times \frac{23}{25} =</math> _____ (mixed number).</p> | <p>(19) <math>4 + 8 + 12 + 16 + 20 + 24 =</math> _____</p> <p>*(20) <math>61 \times 18 \times 49 =</math> _____</p> <p>(21) What number times 3 and added to 18, gives the same result? _____</p> <p>(22) <math>321 \div 7</math> has a remainder of _____</p> <p>(23) <math>3367 \times 14 =</math> _____</p> <p>(24) The ratio of the length to the width of a rectangle is 9:5. Its perimeter is 84 and its area is _____</p> <p>(25) <math>43 \times 43 =</math> _____</p> <p>(26) If <math>x\%</math> of <math>150 = 57</math> then <math>x =</math> _____</p> <p>(27) <math>.43333 \dots =</math> _____ (fraction).</p> <p>(28) The number 120 has _____ positive integral divisors.</p> <p>(29) <math>23\frac{1}{4} + 5 =</math> _____ (mixed number).</p> <p>*(30) <math>15945 \div 19 =</math> _____</p> <p>(31) If <math>3x + 1 = 4x + 5</math> then <math>x =</math> _____</p> <p>(32) <math>4\frac{2}{3} \times 8\frac{2}{3} =</math> _____ (mixed number).</p> <p>(33) If <math>17 = x^2 - y^2</math> and <math>x, y</math> are positive integers then <math>x =</math> _____</p> <p>(34) If <math>A = 2, B = 4</math> and <math>C = 5</math> then <math>AB^3C =</math> _____</p> |
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- (35) If  $x^2 - y^2 = 30$  and  $x + y = 6$  then  $x - y =$  \_\_\_\_\_.
- (36) The cube root of 79,507 is \_\_\_\_\_.
- (37) If 3 A's and 2 B's cost \$6.05 and 2 A's and B cost \$3.65 then A costs \$ \_\_\_\_\_.
- (38) If  $(31)(26) = 62y$  then  $y =$  \_\_\_\_\_.
- (39)  $112 \times 103 =$  \_\_\_\_\_.
- \*(40)  $29 \times 17 \times 19 =$  \_\_\_\_\_.
- (41) If  $4^{x+y} = 9$  and  $4^{x-y} = 4$  then  $4^{2x} =$  \_\_\_\_\_.
- (42) The sum of the roots of  $2x^3 + 2x^2 = x$  is \_\_\_\_\_.
- (43) The next term of 27,24,19,12,3,... is \_\_\_\_\_.
- (44)  $84 \times 86 =$  \_\_\_\_\_.
- (45) If 35 and 43 are in base 9, find the remainder when their sum is divided by 7. \_\_\_\_\_.
- (46)  $16^2 + 59^2 =$  \_\_\_\_\_.
- (47) The sides of a right triangle are integers. If one leg is 11 then the other leg is \_\_\_\_\_.
- (48) If  $1 - x > 2 - 2x$  then  $x >$  \_\_\_\_\_.
- (49) If (3,4) is the midpoint of the line segment through the points (4,7) and (a,b) then  $a =$  \_\_\_\_\_.
- \*(50)  $\sqrt{2000} =$  \_\_\_\_\_.
- (51) If  $(3 + 2i) + (a + bi) = 7 - 3i$  then  $b =$  \_\_\_\_\_.
- (52)  $1 + .5 + .25 + .125 + \dots =$  \_\_\_\_\_.
- (53) If  $\log_x 16 = -2$  then  $x =$  \_\_\_\_\_.
- (54) If  $(3 - 2i)^2 = a + bi$  then  $a =$  \_\_\_\_\_.
- (55) The perimeter of a regular hexagon is 24". Its area is \_\_\_\_\_ sq. in.
- (56) 2 miles = \_\_\_\_\_ feet.
- (57)  $(1 + i) \div (1 - i) = a + bi$  and  $b =$  \_\_\_\_\_.
- (58) If  $43_b = 35$  then  $b =$  \_\_\_\_\_.

- (59)  $3 + 8 + 13 + 18 + \dots + 88 =$  \_\_\_\_\_.
- \*(60)  $14 \times 27 + 15 \times 28 =$  \_\_\_\_\_.
- (61) If  $\log_3 5 = \log_9 x$  then  $x =$  \_\_\_\_\_.
- (62) If  $\tan A = 1$ , A is in QIII then  $A =$  \_\_\_\_\_ radians.
- (63) The sum of the coefficients in the expansion of  $(x + 2y)^3$  is \_\_\_\_\_.
- (64)  $111 \times 213 =$  \_\_\_\_\_.
- (65) The simplified coefficient of the  $x^4 y^2$  term in the expansion of  $(2x - y)^6$  is \_\_\_\_\_.
- (66)  $31_9 \div 4_9 =$  \_\_\_\_\_.
- (67) The odds of winning are 5 to 8. What is the probability of losing? \_\_\_\_\_.
- (68)  $\sin^{-1}(.5) =$  \_\_\_\_\_ degrees.
- (69) Change .44, base 6, to a base 10 fraction. \_\_\_\_\_.
- \*(70)  $142857 \times 15 =$  \_\_\_\_\_.
- (71) Find the value of y if  $x + y = 20$ , the product  $xy^3$  is a maximum and  $x, y > 0$ . \_\_\_\_\_.
- (72) What is the 4<sup>th</sup> triangular number? \_\_\_\_\_.
- (73) If  $f(x) = x^2 - 2$ , find  $f[f(3)]$ . \_\_\_\_\_.
- (74) If  $f(x) = \frac{x+4}{2x-1}$  and  $f^{-1}(x) = \frac{-x+b}{cx+d}$  then  $b =$  \_\_\_\_\_.
- (75)  $14^7 \div 9$  has a remainder of \_\_\_\_\_.
- (76) An urn contains 9 red and x white balls. Find x if the probability of drawing a red ball is 3/7. \_\_\_\_\_.
- (77) If  $1 < x < 4$  then  $x^2 - 1 <$  \_\_\_\_\_.
- (78) The nth term of 4,9,14,19,... is \_\_\_\_\_.
- (79)  $\int_1^8 x^{-2} dx =$  \_\_\_\_\_.
- \*(80)  $34^3 =$  \_\_\_\_\_.